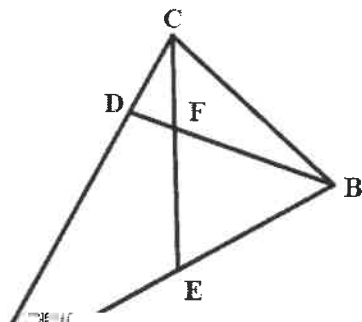


**2017 John O'Bryan Mathematical Competition
Junior-Senior Individual Test**

Directions: Please answer all questions on the answer sheet provided. All answers must be written legibly and in simplest form. ~~Every answer must be written on the answer sheet.~~

2. Given that $i - 2i^2 + 3i^3 - 4i^4 = a + bi$, where $i = \sqrt{-1}$ and a and b are real numbers, find the value of $a^2 - b^2$.
3. The first term of an arithmetic sequence is 32 and the last term is 74. There are 38 terms in the sequence. Find the sum of the 38 terms in this sequence.
4. Find the exact area of an equilateral triangle inscribed in the circle with equation $x^2 + y^2 = 12$.
5. Find the largest number of pigeonholes which 225 pigeons can occupy, given that there must be at least one pigeon in each hole and that no two holes can contain the same number of pigeons.
6. $\triangle ABC$ is isosceles with vertex angle A having a measure of 36° . \overline{CE} bisects $\angle ACB$ and \overline{BD} is one of the trisectors of $\angle ABC$ so that the measure of $\angle CBD$ is less than the measure of $\angle DBA$. Find the degree measure of $\angle CFB$.



7. Find the ordered pair of positive integers (x, y) for which $x^2 - y^2 = 19$.
8. The graph of $4x^2 - y^2 - 8x + 2y = 1$ is rotated 90° clockwise about the origin. Find the coordinates of the center of the new rotated conic. Write your answer as the ordered pair (x, y) .
9. Find the value of k for which $x + 4$ is a factor of $2x^2 + kx - 8$.
10. A bag contains red and green marbles. When two marbles are drawn, the probability that they are both red is equal to the probability that they are both green. The probability of drawing a red marble is 4.

Name: _____ **ANSWERS** _____

Team Code: _____

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Note: All answers must be written legibly and in simplest form. Exact answers are to be given unless otherwise specified in the question. No units of measurement are required. Each problem has the same point-value (1 point).

1. 11

11. 30

2. 0

12. 70

3. 2014

13. 5050

4. $9\sqrt{3}$

14. 6

5. 20

15. $\frac{5}{28}$

6. 120

16. $-4\sqrt{3}$

7. (10,9)

17. 4π

8. (1,-1)

18. 6

9. 6

19. 9

10. 8

20. -3